

Exercise 10

NAME:	MATRICULATION NUMBER:
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RESULTS:

10.1	OF 5 P
10.2	OF 5 P
10.3	OF 5 P
TOTAL	OF 15 P

GENERAL INSTRUCTIONS

- SUBMIT YOUR SOLUTION TO LUCA DONATI (R. 35.17) BEFORE **THURSDAY 09. JULY AT 8.15 AM.**
- FILL OUT THIS COVER SHEET AND SUBMIT IT ALONG WITH YOUR SOLUTION.
- SHOW HOW YOU ARRIVED AT YOUR ANSWER.

10.1 Rotational-vibrational spectrum of $^1\text{H}^{127}\text{I}$ (5 P)

The absorption lines of the rotational-vibrational spectrum of $^{12}\text{C}^{16}\text{O}$ occur at the following wavenumbers

- P-Branch: 2275.90 cm^{-1} , 2263.05 cm^{-1} , 2250.20 cm^{-1} , 2237.35 cm^{-1} ,...
 - R-Branch: 2301.60 cm^{-1} , 2314.45 cm^{-1} , 2327.30 cm^{-1} , 2340.14 cm^{-1} ,...
- (a) Calculate the characteristic vibrational temperature Θ_{vib} and the characteristic rotational temperature Θ_{rot} of $^1\text{H}^{127}\text{I}$. Explain how you arrived at the results.
 - (b) From the characteristic vibrational temperature Θ_{vib} , calculate the ground state vibrational frequency and the bond force constant k .
 - (c) From the characteristic rotational temperature Θ_{rot} , calculate the moment of inertia and the bond length r .
 - (d) Compare your results with tabulated values for $^1\text{H}^{127}\text{I}$.

10.2 Mixing CO and O₂ (5 P)

Consider a container of volume $V = 0.05\text{ m}^3$ which is split into two compartments with volumes $V_1 = V_2 = 0.025\text{ m}^3$ by a wall. The first compartment is filled with 1 mol of $^{16}\text{O}-^{16}\text{O}$. The second compartment is filled with 2 mol of $^{12}\text{C}-^{16}\text{O}$. The temperature is 300 K. The characteristic temperatures for vibration and rotation of the two substances are

- $^{12}\text{C}-^{16}\text{O}$: $\Theta_{\text{vib}} = 3112\text{ K}$ and $\Theta_{\text{rot}} = 2.766\text{ K}$
 - $^{16}\text{O}-^{16}\text{O}$: $\Theta_{\text{vib}} = 2265\text{ K}$ and $\Theta_{\text{rot}} = 2.068\text{ K}$
- (a) Calculate the pressure in the two compartments.
 - (b) Calculate the free energy of mixing.
 - (c) Calculate the partial pressures of $^{16}\text{O}-^{16}\text{O}$ and of $^{12}\text{C}-^{16}\text{O}$ after mixing.
 - (d) Calculate the chemical potential of $^{16}\text{O}-^{16}\text{O}$ and of $^{12}\text{C}-^{16}\text{O}$ in the mixture.

10.3 Entropy of mixing**(5 P)**

Consider two gases A and B with particle numbers N_A and N_B confined to volumes V_A and V_B . These two gases are mixed in volume $V = V_A + V_B$ (analogous to exercise 10.2)

- (a) Give an expression for the entropy of mixing ΔS
- (b) Assume that A is the same gas as B . Given an expression for ΔS .
- (c) Assume that A and B are different particles but that the particles in each gas are distinguishable. Give an expression for ΔS .